# **Volume Worksheet Answers**

## Calculating the Volume to Fill Engineered Objects Geometric Shapes

Prisms, cones and cylinders refer to 3-dimensional (3D) objects that an external (surface) walls that enclose an interior compartment. Often referred to by other names, a "box" is a square or rectangular prism and a "can" is a cylinder. The volume of the compartment depends on the external walls' dimensions.

To simplify the prototype, use either square or rectangular prisms. Calculate the volume needed to fill prism without any objects added. Volume units are written cubed (ex. cubic centimeters written as cm³) or used a "liquid" unit (ex. milliliters). Object(s) added into the internal compartment will reduce the final resin volume as the object(s) takes the resin space.

Cuboid or Rectangular Prism (Box; Ice Cooler)	<ul> <li>four sides (walls)</li> <li>flat sides</li> <li>90° angle at edges</li> <li>space within walls</li> </ul>	b c	Volume (V) = abc  If a=b=c then named <i>Cube</i> or <i>Square</i> . (b is similar to its height)  If two or no measurements equal
Triangular Prism	<ul> <li>three sides</li> <li>polyhedron with five faces</li> <li>right triangular prism has rectangular sides, otherwise called</li> </ul>	h	then named <i>Rectangle</i> .  V= (½ a)(c)(h) where base = (½ a)(c) and height=h
Cylinder (Paint can)	<ul> <li>oblique triangle</li> <li>Circular base exactly over each other with axis at right angles to base is "right cylinder"</li> <li>If one base is displaced sideways call oblique</li> </ul>	h	V = (base)(height) where base=(π)(radius²) & Radius = ½ diameter (d)  V=Base x height = π(r²)(h)



#### Calculate the Volume. $\pi = 3.14$

### **Section A. Paint Containers**

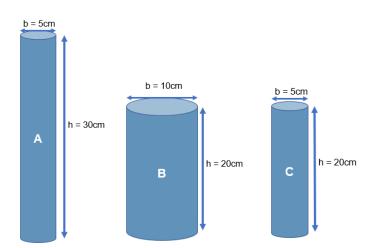
1. Sketch each can and label the canister's base diameter and height. Calculate the maximum amount of paint that each paint canister can store.

Can A: base diameter = 5cm height = 30cm

Can B: base diameter = 10cm height = 20cm

Can C: base diameter = 5cm height = 20cm

Can A: V = 588.75cm<sup>3</sup> Can B: V = 1,570 cm<sup>3</sup> Can C: V = 392.5 cm<sup>3</sup>



2. What is the volume of a cylinder that has a radius of 3 in and a height of 6 in?

V = Base x height = 
$$\pi$$
 (r<sup>2</sup>)(h)= 3.14(3<sup>2</sup>)(6) = 169.56 in<sup>3</sup>

#### Section B. Boxes

1. When preparing for a picnic, an ice cooler is to be filled with drinking water. Which cooler can hold the most water?

Cooler A: a = 40cm

 $V = 64,000 \text{ cm}^3$ 

Cooler A can hold the most water

b = 40 cm

c = 40cm

Cooler B: a = 25cm

 $V = 32,000 \text{ cm}^3$ 

b = 32cmc = 40cm



2. Calculate the volume of a cooler that has the dimensions of width 25 in, length 32 in and height 40 in. What is the volume in inches and centimeters?

```
V= a*b*c = 32,000 in<sup>3</sup>

Conversion factor is 1in = 2.54cm

V = 32,000 in<sup>3</sup> x (2.54cm/in)<sup>3</sup>

V = 524,386 cm<sup>3</sup>
```

- 3. What is the volume of a box with a base of 4 inches by 4 inches and a height of 10 inches?  $V = Base \times height = (4 \times 4) (10) = 160 in^3 (2622cm^3)$
- 4. What is the volume of a box with a base of 8 inches by 8 inches that has a height of 10 inches?  $V = Base \times height = (8 \times 8) (10) = 640 in^3 (10488cm^3)$

# Section C: Triangular Prism with 90-degree angle

1. Calculate the volume of a right triangular prism with sides of 3in x 4in x 5in and a height of 12in.

```
V = Base x height = (1/2 \text{ bh}) (H) = (1/2 \text{ x } 3 \text{ x } 4) (12) = 72 \text{ in}^3 (1180 \text{ cm}^3)
```

2. Calculate the volume of a right triangular prism with sides of 3in x 4in x 5in and a height of 10in

```
V = Base x height = (1/2 \text{ bh}) (H) = (1/2 \times 3 \times 4) (10) = 60 in<sup>3</sup> (983 cm<sup>3</sup>)
```

3. Calculate the volume of a right triangular prism with sides of 5in x 12in x 13in and a height of 12in.

```
V = Base x height = (1/2 \text{ bh}) (H) = (1/2 \times 5 \times 12) (12) = 360 in<sup>3</sup> (5899 cm<sup>3</sup>)
```



